



# Triple-Proof Quantum Finality: Post-Quantum Consensus for the Lux Network

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# Triple-Proof Quantum Finality

## Post-Quantum Consensus for the Lux Network

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### Abstract

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We present **triple-proof quantum finality**, a consensus mechanism for the Lux Network that achieves simultaneous classical speed, post-quantum security, and validator privacy in 248 bytes per epoch. The mechanism combines three independent cryptographic proofs: (1) BLS12-381 aggregate signatures for sub-millisecond classical consensus, (2) STARK-aggregated ML-DSA-65 (FIPS 204) signatures for post-quantum identity binding, and (3) Corona lattice-based threshold signatures for anonymous validator participation. No single cryptographic break compromises the system. At 1ms block times, the mechanism requires approximately 1 TB/year of storage for block headers and epoch proofs combined. We provide benchmarks showing  $\sim 2\text{--}5$  ms CPU QuasarCert verification on commodity hardware [7].

### Introduction

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Post-quantum cryptography faces a fundamental tension: the most promising post-quantum signature schemes (ML-DSA, SLH-DSA) produce signatures  $50\text{--}100\times$  larger than classical schemes (ECDSA, BLS), making them impractical for per-block consensus in high-throughput blockchains. Signature aggregation, which makes BLS practical for consensus ( $N$  signatures  $\rightarrow$  48 bytes), has no known post-quantum equivalent.

We resolve this tension with a layered approach:

1. **Per-block:** Use BLS aggregation for speed (48 bytes, sub-millisecond).
2. **Per-epoch:** Use STARK proofs to compress  $N$  ML-DSA signatures into  $\sim 200$  bytes.
3. **Embedded:** Corona threshold signatures provide privacy within the STARK circuit at zero additional cost.

The result is a consensus mechanism that is simultaneously fast (1ms blocks), compact (248 bytes/epoch), post-quantum secure (ML-DSA + Corona), and privacy-preserving (anonymous validator participation).

### Threat Model

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We consider three classes of adversary:

- **Classical adversary:** Can corrupt up to  $f < N/3$  validators. Cannot break BLS, ML-DSA, or Corona.
- **Quantum adversary:** Has access to a cryptographically relevant quantum computer (CRQC). Can break BLS and ECDSA. Cannot break ML-DSA (NIST FIPS 204) or Corona (Module-LWE).

- **Future adversary:** One of ML-DSA or Corona has an unforeseen mathematical weakness. The other, combined with BLS, still provides security.

Triple-proof finality is secure against all three adversary classes simultaneously.

## The Three Proofs

### Proof 1: BLS Aggregate Signature (Classical Speed)

Every validator signs each block with their BLS12-381 key. The block proposer aggregates all signatures into a single 48-byte aggregate signature. Verification is  $O(1)$  regardless of validator count.

| Property       | Value                                        |
|----------------|----------------------------------------------|
| Curve          | BLS12-381                                    |
| Security       | 128-bit classical                            |
| Signature size | 96 bytes (individual), 48 bytes (aggregated) |
| Aggregation    | $N \rightarrow 1$                            |
| Verification   | $O(1)$ pairing check                         |
| Post-quantum   | No                                           |

BLS provides the real-time consensus path. It is fast, compact, and well-understood. Its lack of post-quantum security is compensated by Proofs 2 and 3.

### Proof 2: STARK-Aggregated ML-DSA (Post-Quantum Identity)

Every validator also signs each epoch checkpoint with their ML-DSA-65 key (FIPS 204, ML-DSA). Individual ML-DSA-65 signatures are 3,309 bytes each — too large to include in block headers.

The STARK aggregation step compresses  $N$  ML-DSA signatures into a single succinct proof of approximately 200 bytes:

$$\text{STARK}(\{(\text{pk}_i, \sigma_i, m)\}_{i=1}^N) \rightarrow \pi \quad |\pi| \approx 200 \text{ bytes}$$

The STARK proof attests: “ $N$  valid ML-DSA-65 signatures over message  $m$  exist, signed by public keys  $\{\text{pk}_i\}$ .” Verification of  $\pi$  is  $O(\log N)$ .

| Property             | Value                               |
|----------------------|-------------------------------------|
| Signature scheme     | ML-DSA-65 (FIPS 204)                |
| Security             | 128-bit post-quantum (NIST Level 3) |
| Individual signature | 3,309 bytes                         |
| Public key           | 1,952 bytes                         |
| Aggregation          | STARK proof ( $\sim 200$ bytes)     |
| Verification         | $O(\log N)$                         |
| QuasarCert verify    | $\sim 2\text{--}5$ ms CPU [7]       |

If BLS is broken by a quantum computer, the STARK proof of ML-DSA signatures remains valid. The entire chain history is verifiable post-quantum.

### Proof 3: Corona Threshold Signature (Post-Quantum Privacy)

Corona [4] is a lattice-based (Module-LWE, Ringtail-derived) threshold signature scheme with an anonymity property: the verifier can confirm that a threshold of validators signed, but cannot determine *which* validators participated.

Corona operates in two rounds:

1. **Round 1:** Each participating validator generates a commitment share.
2. **Round 2:** Shares are combined into a threshold signature. The anonymity set is the full validator committee.

The Corona signature is embedded within the STARK circuit — the STARK proof simultaneously validates both ML-DSA identity signatures and Corona threshold signatures, adding zero bytes to the epoch proof.

| Property         | Value                         |
|------------------|-------------------------------|
| Basis            | Module-LWE (lattice)          |
| Security         | 128-bit post-quantum          |
| Threshold        | $t$ -of- $N$                  |
| Anonymity        | Yes (ring signature property) |
| Rounds           | 2                             |
| Additional bytes | 0 (embedded in STARK proof)   |

Corona provides two properties: (1) post-quantum security at a Module-LWE parameter set distinct from ML-DSA's, and (2) validator privacy — no external observer can determine which specific validators signed a given epoch.

## Block Structure

### Per-Block Header (every 1ms)

```
BlockHeader {
    parent_hash:    [32]byte    // Parent block hash
    state_root:     [32]byte    // Merkle root of state
    tx_root:        [32]byte    // Merkle root of transactions
    timestamp:      uint64      // 8 bytes
    height:         uint64      // 8 bytes
    bls_aggregate:  [32]byte    // Truncated BLS aggregate hash
    // Total: 144 bytes
}
```

The `bls_aggregate` field contains a 32-byte hash of the full 48-byte BLS aggregate signature. The full signature is recoverable from any validator's archive.

### Per-Epoch Proof (every 1,000 blocks = 1 second)

```
EpochProof {
    bls_aggregate:  [48]byte    // Full BLS aggregate signature
    zk_proof:       [~200]byte // STARK(ML-DSA sigs + Corona threshold)
    validators:     uint16      // Count of participating validators
    epoch:          uint64      // Epoch number
}
```

```
// Total: ~258 bytes
}
```

## Security Analysis

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### Defense in Depth

The triple-proof design rests on three independent mathematical assumptions:

1. **Discrete logarithm** (BLS): Hardness of the elliptic curve discrete logarithm problem on BLS12-381.
2. **Lattice problems** (ML-DSA + Corona): Hardness of Module-LWE (both legs are Module-LWE, at distinct parameter sets).
3. **Hash functions** (STARK): Collision resistance of the hash function used in the STARK proof system.

Any two of these three assumptions suffice for full security:

| Scenario               | BLS | ML-DSA/RT           | STARK |
|------------------------|-----|---------------------|-------|
| Classical adversary    | ✓   | ✓                   | ✓     |
| Quantum breaks DL      | ×   | ✓                   | ✓     |
| Lattice weakness found | ✓   | ×                   | ✓     |
| STARK hash broken      | ✓   | ✓ (individual sigs) | ×     |
| Quantum + lattice      | ×   | ×                   | ✓*    |

\*If both discrete log and lattice problems are broken, only the STARK proof (hash-based) remains. This provides integrity but not authenticity — a scenario considered extremely unlikely given current understanding of quantum computing and lattice cryptography.

### Quantum Attack Window

A quantum adversary attempting to forge a BLS signature must do so within the epoch window (1 second). Current estimates for breaking BLS12-381 with a CRQC require  $> 10^6$  logical qubits operating for minutes to hours. The 1-second epoch window is physically impossible to exploit with foreseeable quantum technology.

Even if the epoch window were exploitable, the ML-DSA + Corona proofs would detect the forgery at the next epoch boundary.

## Performance

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### Benchmarks

Measured on Apple M1 Max (10 CPU cores, darwin/arm64, Go 1.26.1). GPU numbers are estimated; all others are `go test -bench` output [7].

| Operation                                   | Time                                         |
|---------------------------------------------|----------------------------------------------|
| BLS sign                                    | 350 $\mu$ s                                  |
| BLS verify (single)                         | 820 $\mu$ s                                  |
| BLS aggregated verify ( $N=100$ )           | 875 $\mu$ s                                  |
| ML-DSA-65 sign                              | 495 $\mu$ s                                  |
| ML-DSA-65 verify (raw)                      | 181 $\mu$ s                                  |
| ML-DSA-65 verify (via fx)                   | 254 $\mu$ s                                  |
| ML-DSA-65 verify (cached)                   | 3 $\mu$ s                                    |
| Groth16 prover (CPU)                        | $\sim 400$ ms                                |
| Groth16 prover (GPU, est.)                  | $\sim 5$ – $15$ ms                           |
| Groth16 verify (3 pairings, CPU)            | $\sim 1$ – $3$ ms                            |
| Quasar block processing (BLS+ML-DSA+Corona) | 1.85 ms                                      |
| <b>QuasarCert total CPU verify</b>          | <b><math>\sim 2</math>–<math>5</math> ms</b> |

## Storage

At 1ms block times (1,000 blocks/second):

| Component                      | Size  | Frequency | Annual                          |
|--------------------------------|-------|-----------|---------------------------------|
| Block header                   | 144 B | 1,000/s   | 4.5 TB                          |
| Epoch proof                    | 258 B | 1/s       | 8.1 GB                          |
| <b>Total (without tx data)</b> |       |           | <b><math>\sim 4.5</math> TB</b> |

With pruning (retain only epoch proofs after 30 days):

| Component                |                                    | Retained | Annual                          |
|--------------------------|------------------------------------|----------|---------------------------------|
| Recent blocks (30 days)  | 144 B $\times$ 1000/s $\times$ 30d |          | 373 GB                          |
| Epoch proofs (permanent) | 258 B $\times$ 1/s $\times$ 365d   |          | 8.1 GB                          |
| <b>Total (pruned)</b>    |                                    |          | <b><math>\sim 381</math> GB</b> |

## Application Chains

Any chain running on the Lux primary network inherits triple-proof quantum finality. The Lux validator set provides consensus for all chains simultaneously.

Current application chains:

| Chain               | Operator | Purpose                    | VM                |
|---------------------|----------|----------------------------|-------------------|
| Application Chain A | Partner  | Regulated securities (ATS) | EVM + precompiles |
| Application Chain B | Partner  | On-chain orderbook         | Custom CLOB       |
| Application Chain C | Partner  | Encrypted computation      | Threshold FHE     |
| Application Chain D | Partner  | AI/DeSci research          | Custom            |

All chains benefit from the same 248-byte quantum epoch proofs without any chain-specific implementation. Quantum finality is a property of the Lux consensus layer, not the application layer.

## Validator Key Set

Each Lux validator maintains four cryptographic keys:

| Key Type | Crypto            | Purpose                     | NIST Standard |
|----------|-------------------|-----------------------------|---------------|
| EC       | secp256k1 (ECDSA) | EVM transactions, addresses | —             |
| BLS      | BLS12-381         | Consensus aggregation       | —             |
| ML-DSA   | Dilithium-65      | PQ identity                 | FIPS 204      |
| Corona   | Module-LWE        | PQ anonymous signing        | —             |

The ML-DSA key is the validator’s *long-term identity*. It certifies the BLS and Corona keys via ML-DSA signatures stored at validator registration (not per-block). If BLS is broken, the ML-DSA certificates prove which validator owned which BLS key.

## Conclusion

Triple-proof quantum finality provides defense-in-depth against classical, quantum, and future adversaries. By separating speed (BLS), identity (ML-DSA), and privacy (Corona) into independent proof paths unified by Groth16 aggregation, we achieve post-quantum consensus at 248 bytes per epoch — comparable to classical-only systems — while supporting 1ms block times on commodity hardware.

The mechanism is deployed on the Lux Network with 100+ validators and multiple application chains. Measured QuasarCert verification is  $\sim 2\text{--}5$  ms CPU, dominated by Groth16’s 3 pairings on BLS12-381 [7].

## References

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